

# GATE-2018

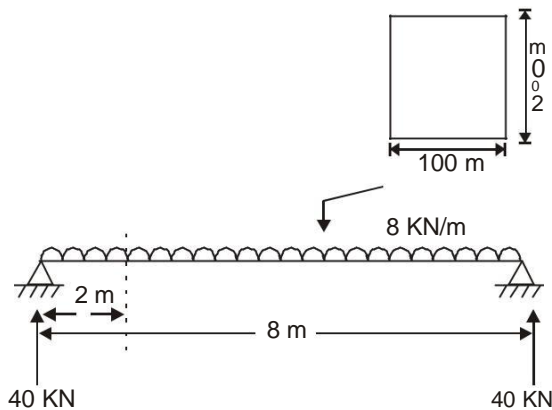
Afternoon Shift-2

**(FOLLOWING QUESTIONS MAY BE CHALLENGED)**

**Section: Civil Engineering**

**GATE (Q.48)** An 8 m long simply-supported elastic beam of rectangular cross-section (100 mm × 200 mm) is subjected to a uniformly distributed load of 10 kN/m over its entire span. The maximum principal stress (in MPa, up to two decimal places) at a point located at the extreme compression edge of a cross-section and at 2 m from the support is

**Sol: (90)**



at 2 m from support,

$$\text{Bending moment, } M = 40 \times 2 - 10 \times 2 \times 1 \\ = 60 \text{ KN-m}$$

$$\text{Shear force, } V = 40 - (10 \times 2) = 20 \text{ KN}$$

At external compression edge (top fibre)

Shear stress  $P = 0$

$$\text{Bending stress, } = \frac{MY}{I}$$

$$= \frac{(60 \times 10^6 \text{ N mm}) \times 100 \text{ mm}}{\frac{100 \times 200^3}{12} \text{ mm}^4}$$

$$= 90 \text{ N / mm}^2$$

$$= 90 \text{ MPa}$$

Since this edge is free from shear stress, hence it is a principal plane.

Thus maximum principal stress = 90 MPa

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## Afternoon Shift-2

### Section : Civil Engineering

**GATE (Q.50)** At a small water treatment plant which has 4 filters, the rate of filtration and backwashing are  $200 \text{ m}^3/\text{d}/\text{m}^2$  and  $1000 \text{ m}^3/\text{d}/\text{m}^2$ , respectively. Backwashing is done for 15 min per day. The maturation, which occurs initially as the filter is put back into service after cleaning, takes 30 min. It is proposed to recover the water being wasted during backwashing and maturation. The percentage increase in the filtered water produced (up to two decimal places) would be \_\_\_\_\_

**Sol: (7.53)**

$$\text{Rate of filtration} = 200 \text{ m}^3 / \text{d} / \text{m}^2$$

$$\text{Backwashing rate} = 1000 \text{ m}^3 / \text{d} / \text{m}^2$$

$$\text{Time for backwashing} = 15 \text{ min/day}$$

$$\text{Time wasted in maturation} = 30 \text{ min}$$

Let the area of filter to be unity

$$\text{Total water to be produced} = 200 \text{ m}^3/\text{d}/\text{m}^2 \times \frac{23.25}{24} = 193.75$$

Water wasted in backwashing

$$\frac{1000 \cdot 15}{24 \cdot 60} = 10.4167 \text{ m}^3$$

Water wasted during maturation

$$= \frac{200 \cdot 30}{24 \cdot 60}$$

$$= 4.1667 \text{ m}^3$$

Total filter water to be produced

$$= 193.75 + 10.4167 + 4.1667$$

$$= 208.3334 \text{ m}^3$$

$$\text{Hence percentage increase in filtered water produced} = \frac{208.3334 - 193.75}{193.75}$$

$$= 7.53\%$$